

Warm-up

Find an equation in standard form for the following:

1) Circle: center $(-2, 4)$, radius 9

2) Parabola: focus $(-1, 3)$, vertex $(-1, 6)$

3) Parabola: focus $(2, -3)$, directrix $(x = 5)$

Find the vertex, directrix and focus:

4) $(x+4)^2 = -2(y+1)$

5) $5y^2 = 20(x+3)$

Homework Section 8.1

In Exercises 11–30, find an equation in standard form for the parabola that satisfies the given conditions.

11. Vertex $(0, 0)$, focus $(-3, 0)$ $y^2 = -12x$

14. Vertex $(0, 0)$, directrix $x = -2$ $y^2 = 8x$

17. Vertex $(0, 0)$, opens to the right, focal width = 8 $y^2 = 8x$

20. Vertex $(0, 0)$, opens upward, focal width = 3 $x^2 = 3y$

23. Focus $(3, 4)$, directrix $y = 1$ $(x - 3)^2 = 6(y - 5/2)$

26. Vertex $(3, 5)$, directrix $y = 7$ $(x - 3)^2 = -8(y - 5)$

30. Vertex $(2, 3)$, opens to the right, focal width = 5

$$30. (y - 3)^2 = 5(x - 2)$$

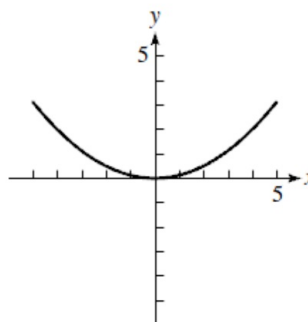
In Exercises 31–36, sketch the graph of the parabola by hand.

32. $x^2 = 8y$

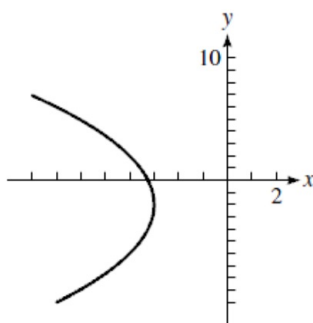
34. $(y + 2)^2 = -16(x + 3)$

36. $(x - 5)^2 = 20(y + 2)$

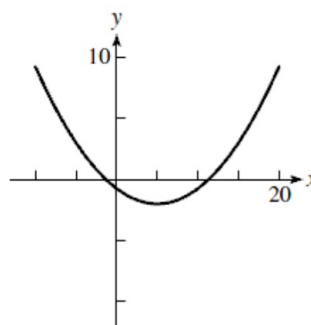
32.



34.



36.



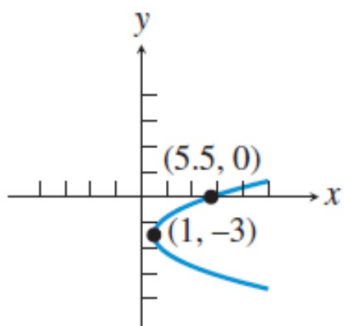
In Exercises 49–52, prove that the graph of the equation is a parabola, and find its vertex, focus, and directrix.

50. $3x^2 - 6x - 6y + 10 = 0$ 50. Completing the square, the equation becomes $(x - 1)^2 = 2(y - 7/6)$,

52. $y^2 - 2y + 4x - 12 = 0$ a parabola with vertex $(1, 7/6)$, focus $(1, 5/3)$ and directrix $y = 2/3$.

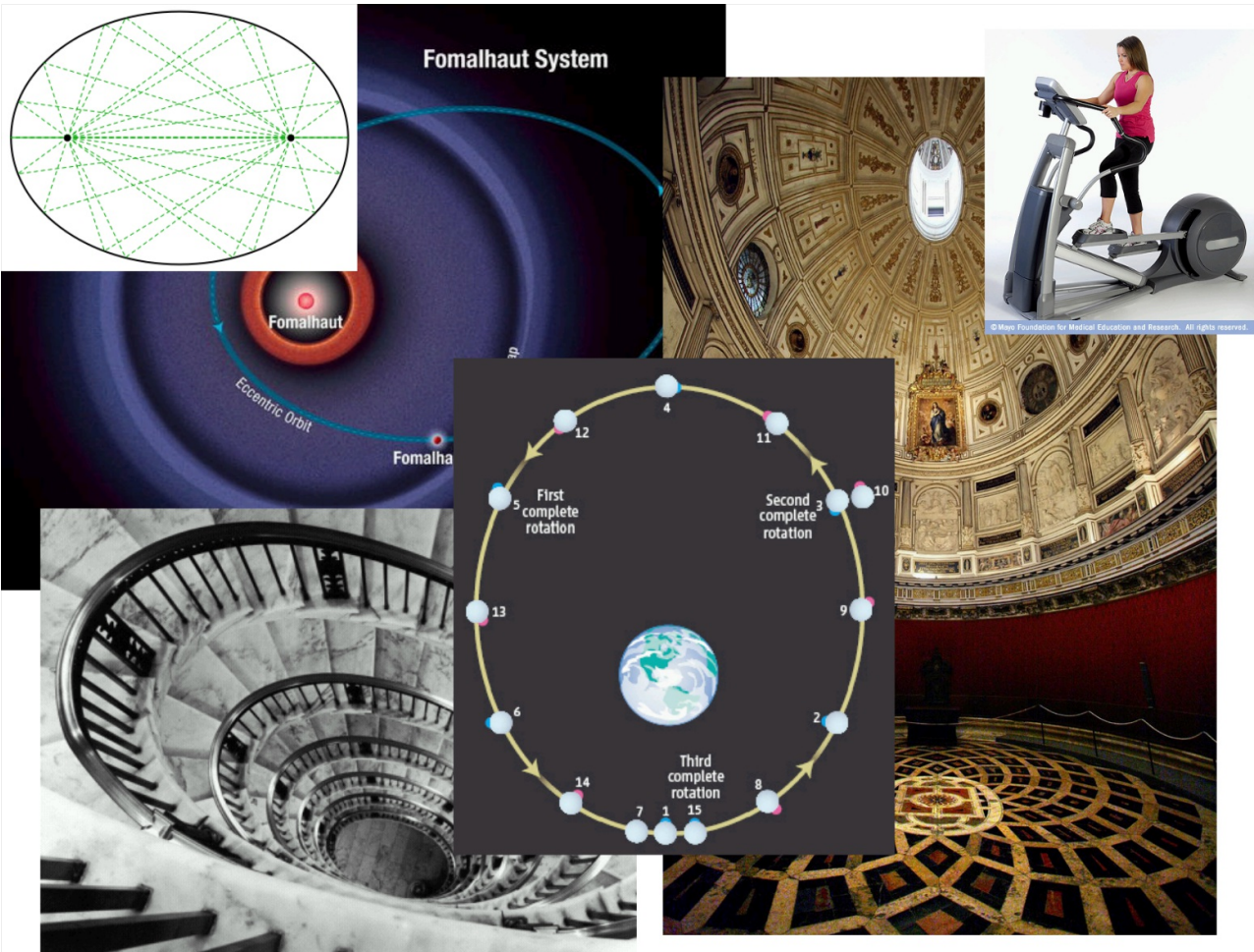
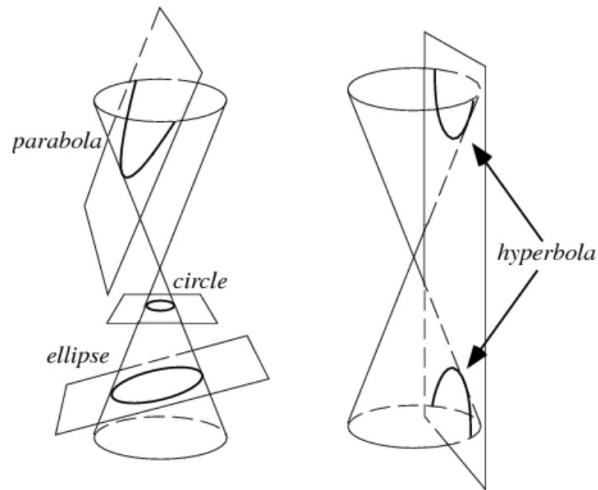
52. Completing the square, the equation becomes $(y - 1)^2 = -4(x - 13/4)$,
vertex $(13/4, 1)$, focus $(9/4, 1)$, and directrix $x = 17/4$.

54.



$(y + 3)^2 = 2(x - 1)$

Diagramming an ELLIPSE!!



8-2 Objective: Graph and write an equation for an ellipse.

An ellipse is the set of all points in a plane such that the sum of the distances from two fixed points (foci) is constant.

Major Axis: longest axis (Vertices)



Minor Axis: shortest axis (Co-Vertices)

The two axes intersect at the center of the ellipse.

What is the standard form of a vertical ellipse? $\frac{(x - h)^2}{b^2} + \frac{(y - k)^2}{a^2} = 1$



What is the standard form of a horizontal ellipse? $\frac{(x - h)^2}{a^2} + \frac{(y - k)^2}{b^2} = 1$



How do you determine "a" and "b"? $a > b$

Center (h, k)

Length of major axis 2a

Length of minor axis 2b

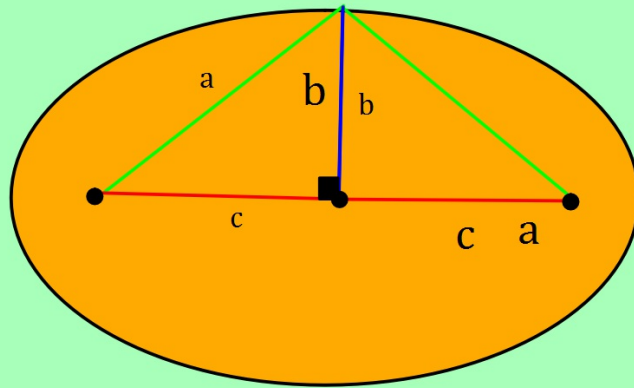
Eccentricity:

$$\frac{c}{a}$$

*0 < e < 1
closer to center*

How to find the Foci??

$$c^2 = a^2 - b^2$$



3. Find each of the following ellipse:

$$\frac{x^2}{5} + \frac{y^2}{9} = 1$$

b² a²

Length of the major axis: 6

Length of the minor axis: $2\sqrt{5}$

Foci: $(0, \pm 2)$

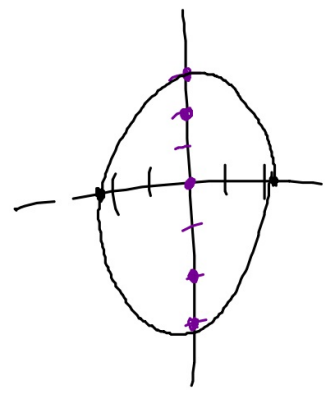
Center: $(0, 0)$

$$c^2 = a^2 - b^2$$

$$c^2 = 9 - 5$$

$$c^2 = 4$$

$$c = 2$$



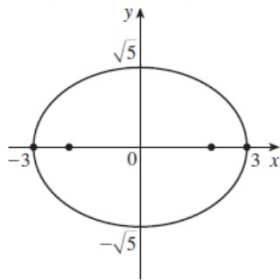
11-16 ■ Find the vertices and foci of the ellipse and sketch its graph.

11. $\frac{x^2}{9} + \frac{y^2}{5} = 1$

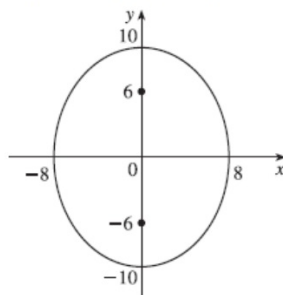
12. $\frac{x^2}{64} + \frac{y^2}{100} = 1$

13. $\frac{4x^2}{16} + \frac{y^2}{16} = \frac{16}{16}$

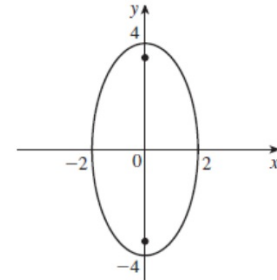
11. $(\pm 3, 0), (\pm 2, 0)$



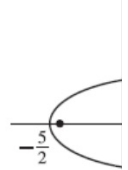
12. $(0, \pm 10), (0, \pm 6)$



13. $(0, \pm 4), (0, \pm 2\sqrt{3})$



14. $(\pm \frac{5}{2}, 0)$



In Exercises 37-40, find the center, vertices, and foci of the ellipse.

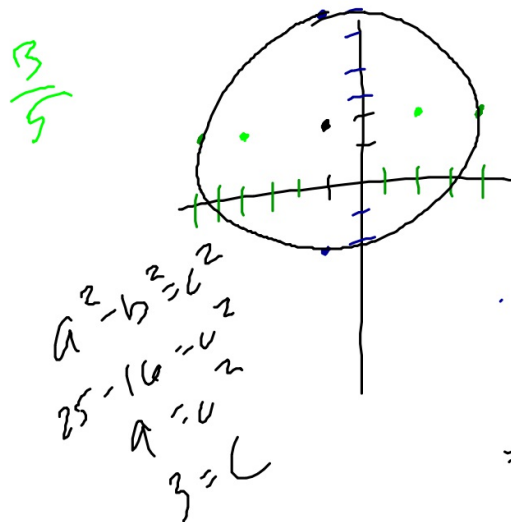
37. $\frac{(x+1)^2}{25} + \frac{(y-2)^2}{16} = 1$

Length of the major axis: 10

Length of the minor axis: 8

Foci: $(-4, 2)$ $(2, 2)$

Center: $(-1, 2)$

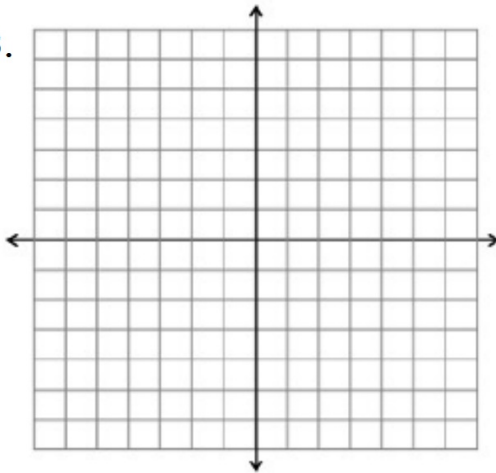


Sketch the ellipses by hand and give the foci

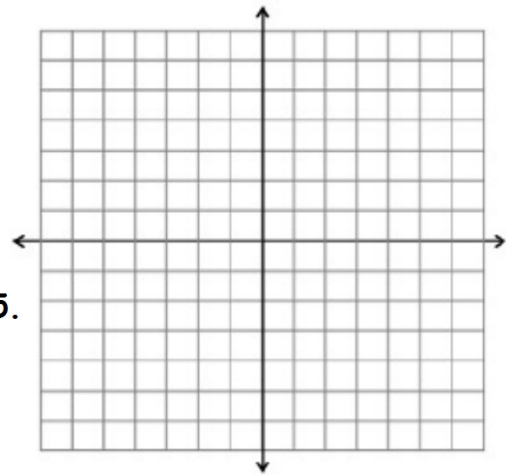
13. $\frac{y^2}{9} + \frac{x^2}{4} = 1$

15. $\frac{(x+3)^2}{16} + \frac{(y-1)^2}{4} = 1$

13.

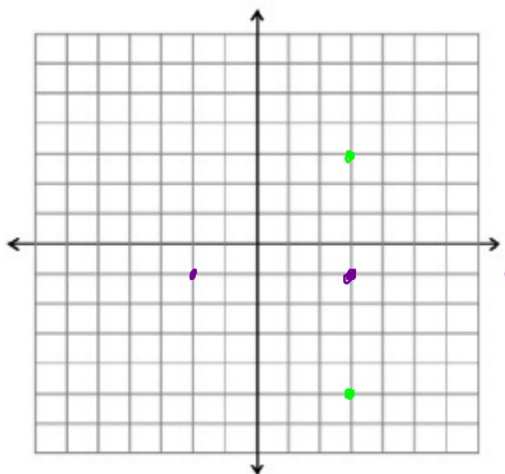


15.



Finding an Equation of an Ellipse

Find the standard form of the equation for the ellipse whose major axis has endpoints $(-2, -1)$ and $(8, -1)$, and whose minor axis has length 8.

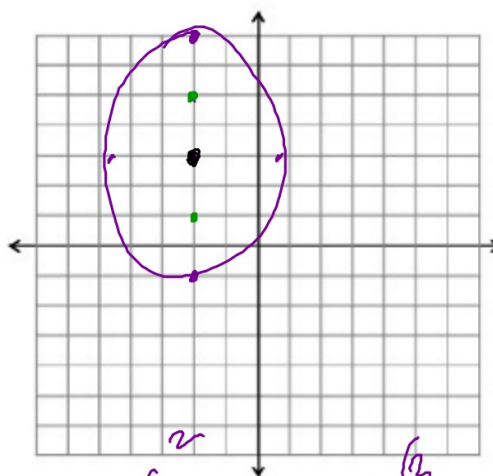


$c = (3, -1)$
 $\frac{(x-3)^2}{25} + \frac{(y+1)^2}{16} = 1$

6. Write the equation of the ellipse:

The foci are $(-2, 1)$ and $(-2, 5)$; the major axis endpoints are $(-2, -1)$ and $(-2, 7)$.

$$\frac{(x+2)^2}{12} + \frac{(y-3)^2}{16} = 1$$



$$\begin{aligned} a^2 - b^2 &= c^2 \\ 16 - b^2 &= 4 \\ b^2 &= 12 \quad b = 2\sqrt{3} \end{aligned}$$

31–48 ■ Find an equation for the conic that satisfies the given conditions.

37. Ellipse, foci $(\pm 2, 0)$, vertices $(\pm 5, 0)$

38. Ellipse, foci $(0, \pm 5)$, vertices $(0, \pm 13)$

39. Ellipse, foci $(0, 2)$, $(0, 6)$ vertices $(0, 0)$, $(0, 8)$

40. Ellipse, foci $(0, -1)$, $(8, -1)$, vertex $(9, -1)$

41. Ellipse, center $(2, 2)$, focus $(0, 2)$, vertex $(5, 2)$

$$36. 2x^2 + 4x - y + 3 = 0 \quad 37. \frac{x^2}{25} + \frac{y^2}{21} = 1$$

$$38. \frac{x^2}{144} + \frac{y^2}{169} = 1 \quad 39. \frac{x^2}{12} + \frac{(y-4)^2}{16} = 1$$

$$40. \frac{(x-4)^2}{25} + \frac{(y+1)^2}{9} = 1 \quad 41. \frac{(x-2)^2}{9} + \frac{(y-2)^2}{5} = 1$$

In Exercises 37–40, find the center, vertices, and foci of the ellipse.

$$37. \frac{(x+1)^2}{25} + \frac{(y-2)^2}{16} = 1$$

Try this one! prove that the graph of the equation is an ellipse, and find its vertices, foci, and eccentricity.

$$9x^2 + 4y^2 - 18x + 8y - 23 = 0$$

$$9x^2 - 18x + 4y^2 + 8y = 23$$

$$9(x^2 - 2x + 1) + 4(y^2 + 2y + 1) = 23 + 9 + 4$$

$$\frac{9(x-1)^2}{36} + \frac{4(y+1)^2}{36} = \frac{36}{36} \quad \frac{(x-1)^2}{4} + \frac{(y+1)^2}{9} = 1$$

9. Find the coordinates of the center and foci and the lengths of the major and minor axis of the ellipse with equation

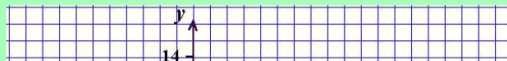
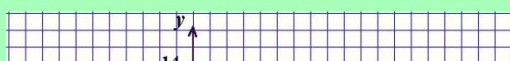
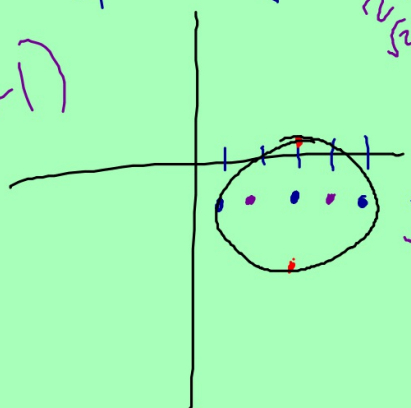
~~15. $9x^2 - 18x + 4y^2 = 27$~~

16. $x^2 + 2y^2 - 6x + 4y + 7 = 0$

$\frac{(x-3)^2}{4} + \frac{2(y+1)^2}{4} = \frac{4}{4}$

$\frac{(x-3)^2}{4} + \frac{(y+1)^2}{2} = 1$
 $2 = 2$
 $(\sqrt{2})^2$

$(3 \pm \sqrt{2}, -1)$



In Exercises 11–16, sketch the graph of the ellipse by hand.

12. $\frac{x^2}{81} + \frac{y^2}{25} = 1$

14. $\frac{y^2}{49} + \frac{x^2}{25} = 1$

16. $\frac{(x-1)^2}{2} + \frac{(y+3)^2}{4} = 1$

In Exercises 21–36, find an equation in standard form for the ellipse that satisfies the given conditions.

21. Major axis length 6 on y-axis, minor axis length 4

24. Foci $(0, \pm 3)$, major axis length 10

27. Major axis endpoints $(0, \pm 6)$, minor axis length 8

30. Minor axis endpoints $(\pm 12, 0)$, major axis length 26

33. The foci are $(1, -4)$ and $(5, -4)$; the major axis endpoints are $(0, -4)$ and $(6, -4)$.

36. The major axis endpoints are $(-5, 2)$ and $(3, 2)$; the minor axis length is 6.

In Exercises 37–40, find the center, vertices, and foci of the ellipse.

38. $\frac{(x-3)^2}{11} + \frac{(y-5)^2}{7} = 1$

40. $\frac{(y-1)^2}{25} + \frac{(x+2)^2}{16} = 1$

In Exercises 45–48, prove that the graph of the equation is an ellipse, and find its vertices, foci, and eccentricity.

46. $3x^2 + 5y^2 - 12x + 30y + 42 = 0$

48. $4x^2 + y^2 - 32x + 16y + 124 = 0$

In Exercises 49 and 50, write an equation for the ellipse.

50.

