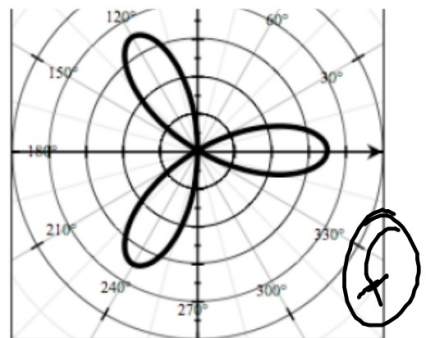
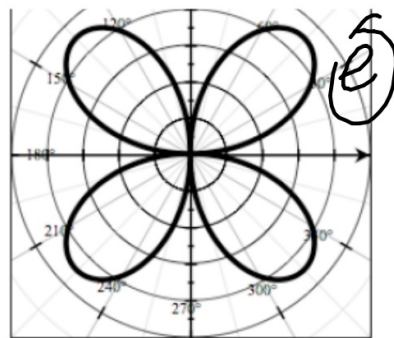
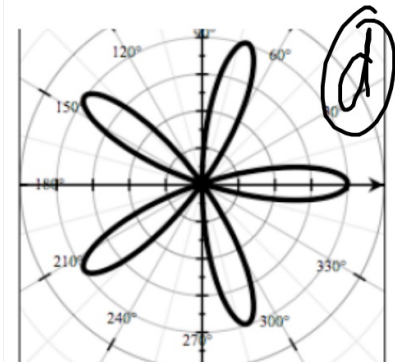


Match the polar equations with their graphs below.

MATCH GRAPH

- | | | | |
|--------------------------------|------------------------------|-------------------------------|---------------------------------|
| 1) $r = 2.5 + 2.5 \sin \theta$ | 2) $r = 3$ | a) 3) $r = 3.5 \sin 3\theta$ | c) 4) $r = 4.5 \sin 2\theta$ |
| 5) $r = 4.5 \cos 2\theta$ | 6) $r = 1.5 + 2 \cos \theta$ | 7) $r = -3 \sin \theta$ | 8) $r = 2 - \sin \theta$ |
| 9) $r^2 = 16 \sin 2\theta$ | d) 10) $r = 4 \cos 5\theta$ | f) 11) $r = 3.5 \cos 3\theta$ | 12) $r = 2.5 - 2.5 \cos \theta$ |
| 13) $r = 3 \cos \theta$ | 14) $r = 1 + 4 \sin \theta$ | c) 15) $r = 4.5 \sin 6\theta$ | 16) $r = .5\theta$ |



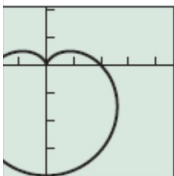
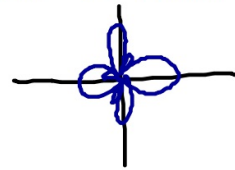
Page 548
9-12, 46, 48

In Exercises 45–48, find the length of each petal of the polar curve.

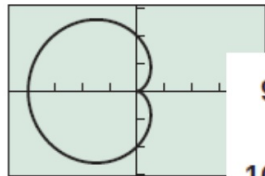
45. $r = 2 + 4 \sin 2\theta$
47. $r = 1 - 4 \cos 5\theta$

46. $r = 3 - 5 \cos 2\theta$
48. $r = 3 + 4 \sin 5\theta$

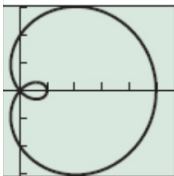
Exercises 9–12, match the equation with its graph without using a graphing calculator.



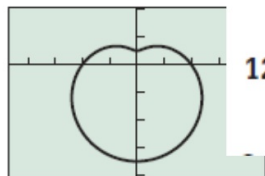
(a) $r = 2 - 2 \sin \theta$



(b) $r = 2 - 2 \cos \theta$



(c) $r = 2 + 3 \cos \theta$



(d) $r = 2 + 3 \sin \theta$

9. Does the graph of $r = 2 + 2 \sin \theta$ or $r = 2 - 2 \cos \theta$ appear in the figure? Explain. **Graph (b) is $r = 2 - 2 \cos \theta$.**
10. Does the graph of $r = 2 + 3 \cos \theta$ or $r = 2 - 3 \cos \theta$ appear in the figure? Explain. **Graph (c) is $r = 2 + 3 \cos \theta$.**
11. Is the graph in (a) the graph of $r = 2 - 2 \sin \theta$ or $r = 2 + 2 \cos \theta$? Explain. **Graph (a) is $r = 2 - 2 \sin \theta$.**
12. Is the graph in (d) the graph of $r = 2 + 1.5 \cos \theta$ or $r = 2 - 1.5 \sin \theta$? Explain. **Graph (d) is $r = 2 - 1.5 \sin \theta$.**

Convert from Polar to Rectangular coordinates

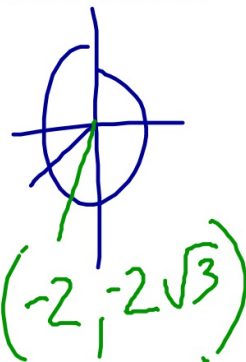
Find exact answer (no decimals)

1) $(-3, 7\pi/6)$

$(-3\cos\frac{7\pi}{6}, -3\sin\frac{7\pi}{6})$

$-3(\frac{-1}{2})$
2) $(4, 240^\circ)$

$-3(\frac{-\sqrt{3}}{2})$ $(\frac{3\sqrt{3}}{2}, \frac{3}{2})$



Convert from Rectangular to Polar coordinates

Find the answer when r and θ are both positive and both negative

1) $(-2, 6)$

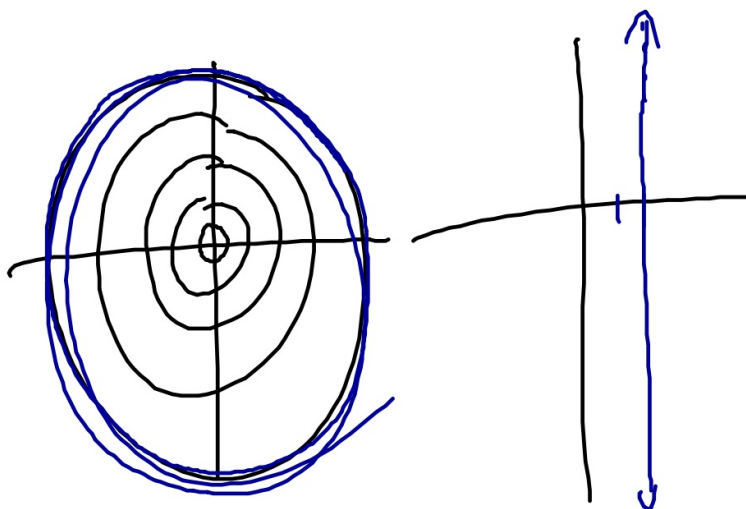
$(2\sqrt{10}, 108.4^\circ)$ $(-2\sqrt{10}, -71.6^\circ)$

2) $(-3, -9)$

$(3\sqrt{10}, 251.6^\circ)$ $(-3\sqrt{10}, 71.6^\circ)$

Analyzing graphs of $r =$ and $\theta =$

$r = 5$
 $x^2 + y^2 = 25$



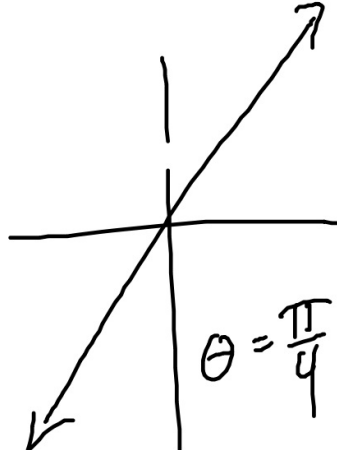
Analyzing graphs of $r =$ and $\theta =$

$$\frac{y}{x} = \frac{x}{x}$$

$$\frac{y}{x} = 1$$

$$\frac{r \sin \theta}{r \cos \theta} = 1$$

$$\tan \theta = 1$$

$$\theta = \frac{\pi}{4}, \frac{5\pi}{4}$$


Analyzing graphs of $r =$ and $\theta =$

$$\theta = \pi/3$$

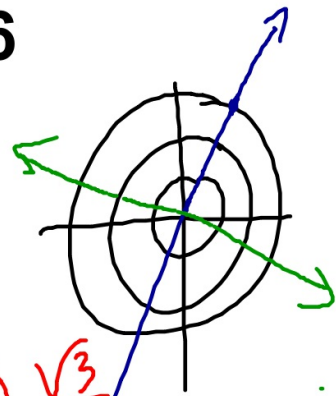
$$y = \frac{\sqrt{3}}{2}x$$

$$y = \sqrt{3}x$$

$$\theta = 5\pi/6$$

$$y = \frac{1}{2}x$$

$$\frac{1}{2}x = \frac{r}{\sqrt{3}} \Rightarrow \frac{1}{\sqrt{3}} = \frac{r}{\sqrt{3}} \Rightarrow r = 1$$



Converting Polar/Rectangular equations

$$r = 4\sin\theta$$

$$r^2 = 4r\sin\theta$$

$$x^2 + y^2 = 4y$$

$$x^2 + y^2 - 4y = 0$$

$$x^2 + (y^2 - 4y + 4) = 0 + 4$$

$$x^2 + (y-2)^2 = 4$$

$$(2, 2) \quad r=2$$

Converting Polar/Rectangular equations

$$r = (4\cos\theta + 8\sin\theta)$$

$$r^2 = 4r\cos\theta + 8r\sin\theta$$

$$x^2 + y^2 = 4x + 8y$$

$$(x-2)^2 + (y-4)^2 = 20$$

Converting Polar/Rectangular equations

~~1) $r = 4$~~

2) $r = 6$
 $x^2 + y^2 = 36$

3) $\theta = \pi/6$
 $y = \frac{\sqrt{3}}{3}x$ $\frac{1}{\frac{\sqrt{3}}{2}}$

4) $r = 5\cos\theta$
 $(x-2.5)^2 + y^2 = 6.25$

5) $r = 3\sec\theta$ $r = 3 \frac{1}{\cos\theta}$
 $x = 3$ $r\cos\theta = 3$

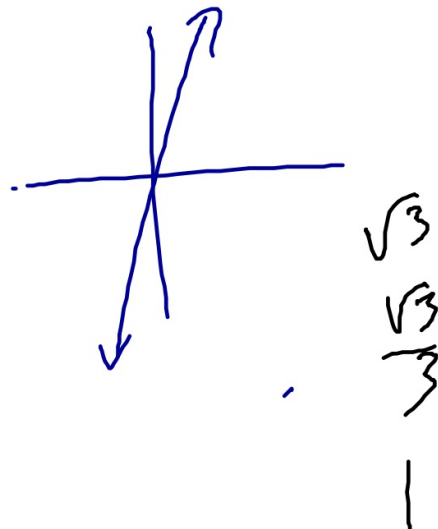
6) $r = \frac{4}{(3\cos\theta + \sin\theta)}$
 $3r\cos\theta + r\sin\theta = 4$
 $3x + y = 4$

Converting Polar/Rectangular equations

$y = \sqrt{3}x$ $\tan\theta = \sqrt{3}$

$\theta = \frac{\pi}{3}$

$\frac{y}{x} = \sqrt{3}$



Converting Polar/Rectangular equations

$$4x - 2y = 7$$

$$\begin{aligned} 4r\cos\theta - 2r\sin\theta &= 7 \\ r(4\cos\theta - 2\sin\theta) &= 7 \end{aligned}$$

$$r = \frac{7(\text{seven})}{4\cos\theta - 2\sin\theta}$$

Converting Polar/Rectangular equations

$$(x - 4)^2 + (y + 1)^2 = 17$$

$$x^2 - 8x + 16 + y^2 + 2y + 1 = 17$$

$$x^2 - 8x + y^2 + 2y = 0$$

$$x^2 + y^2 = 8x - 2y$$

$$\frac{r^2}{r} = \frac{8r\cos\theta}{r} - \frac{2r\sin\theta}{r}$$

$$r = 8\cos\theta - 2\sin\theta$$

In Exercises 35–42, convert the polar equation to rectangular form and identify the graph. ~~Support your answer by graphing the polar equation.~~

35. $r = 3 \sec \theta$

36. $r = -2 \csc \theta$

37. $r = -3 \sin \theta$

38. $r = -4 \cos \theta$

39. $r \csc \theta = 1$

40. $r \sec \theta = 3$

~~41.~~ $r = 2 \sin \theta - 4 \cos \theta$

~~42.~~ $r = 4 \cos \theta - 4 \sin \theta$

In Exercises 43–50, convert the rectangular equation to polar form.

~~Graph the polar equation.~~

~~43.~~ $x = 2$

44. $x = 5$

45. $2x - 3y = 5$

~~46.~~ $3x + 4y = 2$

~~47.~~ $(x - 3)^2 + y^2 = 9$

48. $x^2 + (y - 1)^2 = 1$

~~49.~~ $(x + 3)^2 + (y + 3)^2 = 18$

~~50.~~ $(x - 1)^2 + (y + 4)^2 = 17$