

Warm up

1) What value of x makes the expression true?

a) $5^x = 125$

b) $2^x = 1/32$

c) $(-3)^x = -243$

2) Expand $y = \log(x^2 y^3)$

3) Condense $f(x) = 2 \log_4(x-1) - 4 \log_4(x+3)$

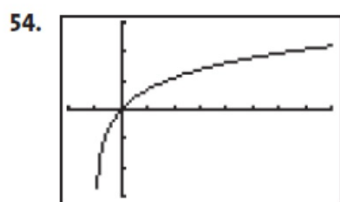
4) Change to exponential form: $\log_3 81 = 2x$

7. $\log 10^3$ 3

20. $5^{\log_5 8}$ 8

34. $\log x = 4$ 10,000

22. $10^{\log 14}$ 14

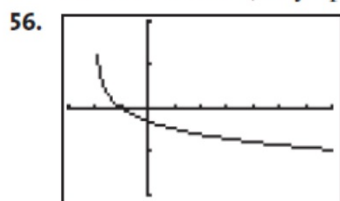


$[-2, 8]$ by $[-3, 3]$

Domain: $(-1, \infty)$; Range: $(-\infty, \infty)$; Continuous;
 Always decreasing; Not symmetric; Not bounded;
 No local extrema; Asymptote: $x = -1$; $\lim_{x \rightarrow \infty} f(x) = \infty$

In Exercises 53–58, graph the function, and analyze it for domain, range, continuity, increasing or decreasing behavior, boundedness, extrema, symmetry, asymptotes, and end behavior.

54. $f(x) = \ln(x + 1)$



$[-3, 7]$ by $[-2, 2]$

Domain: $(-2, \infty)$; Range: $(-\infty, \infty)$; Continuous;
 Always decreasing; Not symmetric; Not bounded;
 No local extrema; Asymptote: $x = -2$; $\lim_{x \rightarrow \infty} f(x) = -\infty$

56. $f(x) = -\log(x + 2)$

$$8. \log xy^3 = \log x + \log y^3 = \log x + 3 \log y$$

$$14. \log x + \log 5 = \log 5x$$

$$19. 2 \ln x + 3 \ln y = \ln x^2 + \ln y^3 = \ln (x^2 y^3)$$

$$24. \log_5 19 \quad 1.8295$$

$$27. \log_{0.5} 12 \quad -3.5850$$

$$30. \log_7 x = \frac{\ln x}{\ln 7}$$

$$34. \log_4 x = \frac{\log x}{\log 4}$$

$$35. \log_{1/2}(x + y) = \frac{\log(x + y)}{\log(1/2)} = -\frac{\log(x + y)}{\log 2}$$

Objective:

Solving exponential and Log equations



Solving Exponential Equations with like bases

STEPS

1. Get the same base on each side.
2. If $b^x = b^y$, then $x=y$.
3. Solve for the variable.
4. Check please!

$$\frac{1}{25} = 125^{2x+3}$$

$$5^{-2} = (5^3)^{2x+3}$$

$$5^{-2} = 5^{6x+9}$$

Handwritten work for a different problem:

$$3^{2x} = 81$$

$$3^{2x} = 3^4$$

$$2x = 4$$

$$x = 2$$

$$3^{5x} = 9^{2x-1}$$

$$3^{5x} = (3^2)^{2x-1}$$

$$3^{5x} = 3^{4x-2}$$

$$5x = 4x - 2$$

$$x = -2$$

$$2^2 \rightarrow 2^7$$

$$3^2 \rightarrow 3^5$$

$$4^2 \rightarrow 4^4$$

$$5^2 \rightarrow 5^4$$

$$6x+9 = -2$$

$$6x = -11$$

$$x = -11/6$$

Practice:

1. $2^{x+1} = 4^{-1}$

2. $\left(\frac{1}{3}\right)^3 = 9^x$

How to...

Evaluate Logarithmic Expressions

GUIDED PRACTICE:

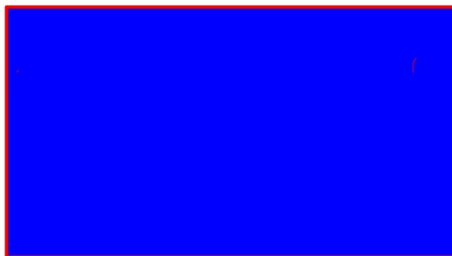
Evaluate each expression.

7. $\log_3 243 = x$

$$\begin{array}{l} b^a = c \\ 3^x = 243 \\ 3^x = 3^5 \end{array}$$

STEPS

1. set $\log_b a$ equal to x
2. change to exponential form $b^x = a$
3. get the bases the same
4. solve for x



$x = 5$

3. $\log_2 32 = 3x$

b
a
s
e

a
n
s
w
e
r

e
x
p.

$$2^{3x} = 32$$

$$2^{3x} = 2^5$$

$$x = \frac{5}{3}$$



What if you cannot get the same base in an exponential equation $b^x = a$?

- *Remember...*

The Power Property of Logarithms says:

$$\log_7 x^2$$
$$= 2 \log_7 x$$




$n \log_b m$ changes to $\log_b m^n$ (power up)

- Well, it works the other way, too:

$\log_b m^n$ changes to $n \log_b m$ (power down)

GUIDED PRACTICE

Solve each equation. Round to four decimal places.

2. $3^x = 11$  You cannot get the same base, so take the log of each side!



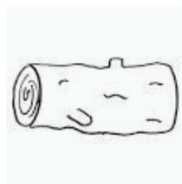
$$\begin{aligned} \log 3^x &= \log 11 \\ x \log 3 &= \frac{\log 11}{\log 3} = 2.1827 \end{aligned}$$

● **CALCULATOR TIP** $\log(11)$ ENTER \div $(\log(3))$ ENTER

TI: blue keystrokes; **CASIO:** blue AND red keystrokes

BOTH: *It is important to close parentheses after the number AND always follow \div by the left parentheses (*

3. $5^{2x} = 32$



4. $3^{n+1} = 7$

How to solve a logarithmic equation:



GUIDED PRACTICE:
Solve.

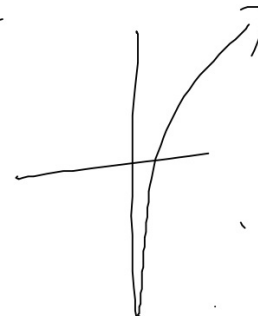
1. $\log_3 5 + \log_3 x = \log_3 10$

$$\log_3 5x = \log_3 10$$

$$5x = 10$$

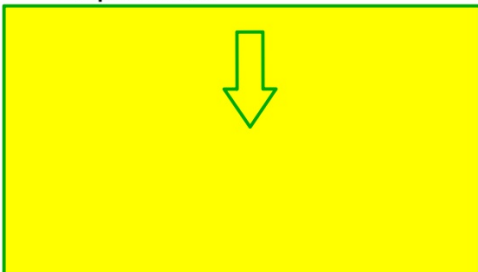
$$x = 2$$

$$x = \frac{10}{5}$$



STEPS:

1. Condense the logarithms
2. If $\log_b a = p$ then change to exponential form and solve.
3. If $\log_b x = \log_b y$, then $x = y$.
4. Solve.
5. CHECK! Remember for $\log_b a = p$, both a and b must be positive!!



5. $\log_2 x + \log_2 (x + 2) = 3$



6. $\log_{10} 16 - \log_{10} 2x = \log_{10} 2$

7. $4 \log_2 x + \log_2 5 = \log_2 405$

8. $3 \log_2 x - 2 \log_2 5x = 2$



How to...

Solve Logarithmic Equations using Exponentiation

Raise both sides to the same base.

- This is called exponentiation.

- Remember...

A base raised to a log with the same base rule:

$$b^{\log_b x} = x$$

- Therefore,
- simplifies to $x = 10^a$

